Catalog Description: The rst course in a three term sequence in applied partial di erential equations. Modelling physical systems using di erential equations, classifying di erential equations and introduction to the methods of solving partial di erential equations (separation of variables, Fourier series, transform methods).

Course Objectives: After completing this course, students will be able to

- 1. Formulate a model for systems for partial di erential equations including but not limited to the Heat, Wave, Laplace, and Poisson equations in one and two dimensions.
- 2. Transform an equation or operator from one geometry to another.
- 3. Classify systems of partial di erential equations.
- 4. Solve partial di erential equations.
- 5. Graph analytical solutions to the following set of example problems.

Learning Outcomes and Performance Criteria

1. Formulate boundary value problems using appropriate coordinates.

Core Criteria:

- (a) Formulate the proper equation and conditions (initial and boundary) for a cylindrical, homogeneous, isotropic rod with at ends and given some initial temperature distribution and boundary conditions.
- (b) Formulate the proper equation and conditions (initial and boundary) for a string with uniform density and tension and a given some initial con guration and boundary conditions.
- (c) Formulate the proper equation and boundary conditions for the steady-state temperature of a thin circular disc given boundary conditions.
- (d) Formulate the proper equation and conditions (initial and boundary) for a circular membrane with uniform density and tension given some initial con guration and boundary conditions.
- (e) Choose the appropriate coordinate system for a given geometry.

Additional Criteria:

- (a) Formulate the proper equation and conditions (initial and boundary) for other domains given some initial temperature distribution or initial con guration and boundary conditions.
- (b) Given the proper equation and conditions for some physical system, reformulate the equation and/or conditions given some change(s) to the system.
- 2. Transform an equation or operator from one geometry to another.

Core Criteria:

- (a) Transform the 2D heat equation from Cartesian to Polar coordinates.
- (b) Transform the 2D wave equation from Cartesian to Polar coordinates.

Additional Criteria:

- (a) Transform the 3D heat equation from Cartesian to Spherical coordinates.
- (b) Transform a 2D Poisson Equation from Cartesian to Polar Coordinates.
- 3. Classify di erential equations.

Core Criteria:

- (a) Given a di erential equation, determine if the equation is linear or non-linear.
- (b) Given a di erential equation, determine if the equation is parabolic, hyperbolic, or elliptic.
- (c) Given a di erential equation, determine if the equation is homogeneous or non-homogenous.
- 4. Solve one and two dimensional partial di erential equations of the heat, wave, and Laplace type in both cartesian and polar coordinates.

Core Criteria:

- (a) Use separation of variables to transform a partial di erential equation, in a given geometry, into a set of equivalent ordinary di erential equations.
- (b) Properly assign initial conditions and boundary values to their respective ordinary di erential equations.
- (c) Use eigenvalues, eigenfunctions and initial-value solution techniques to solve the set of ordinary di erential equations that result from a partial di erential equation. This includes Fourier Series as appropriate.
- (d) Use superposition properly to construct a partial di erential equation solution.
- (e) Use the series form of a forcing function to equate like terms and nd unknown constants for non-homogeneous equations.
- (f) Given a partial di erential equation, show via substitution and di erentiation that a solution solves (or does not solve) an equation of interest.

Additional Criteria:

- (a) Given the proper classi cation, explain the most likely solution method.
- (b) Use the method of characteristics to solve partial di erential equations.
- (c) Use Fourier Transforms to solve partial di erential equations.
- 5. Graph analytical solutions to the following set of example problems.

Core Criteria:

- (a) 1D wave equation.
- (b) 1D heat equation
- (c) 2D Laplace equation in cartesian and polar coordinates.

And one from the following list.

(a) 2D wave equation in cartesian and polar coordinates.