MATH 361 : Statistical Methods I (4-0-4) 01-24-2020

Catalog Description: Descriptive statistics, experimental design, introduction to probability, common probability distributions, random variables, sampling distributions, hypothesis testing and con dence intervals for means using one and two samples, simple linear regression.

Course Objectives: After completing this course, students will be able to

- 1. Describe patterns and departures from patterns in data.
- 2. Use probability rules and distributions, including the binomial and normal distributions, to solve problems.
- 3. Perform statistical inference.
- 4. Draw an appropriate conclusion based on the results of statistical analysis and the study design.

Learning Outcomes and Performance Criteria

- 1. Identify and describe elements of experimental and observational design. Core Criteria:
 - (a) Describe the importance of randomization and its e ect on both variation and bias of data.
 - (b) Describe sampling techniques within an observational design, including but not limited to: Simple Random, Strati ed Sampling, and Cluster Sampling.
 - (c) Identify experimental units and variables within a study, classifying the variable type as continuous numerical, discrete numerical, ordinal categorical, nominal categorical, or binary.
 - (d) Classify what role variables have within a sampling design: explanatory, response, and potential confounding e ects (strata, blocking, or covariates).
 - (e) Identify categorical variables and their levels for a statistical experiment.

2. Organize and describe data with numerical measures.

Core Criteria:

- (a) Calculate the mean.
- (b) Compare and contrast two data sets in terms of their means, variances, and standard deviations.
- (c) Calculate the ve number summary.
- (d) Answer questions about a data set based on the ve number summary.
- (e) Calculate the linear correlation coe cient.
- (f) Calculate the least squares regression line.
- (g) Compare and contrast the correlation coe cient for two data sets (strength and direction).
- (h) Interpret the slope of a least squares regression line in terms of the variables.
- (i) Interpret the coe cient of determination as the percentage of variation in the response variable explained by the linear model.

Additional Criteria:

- (a) Calculate the coe cient of determination.
- (b) Calculate the mode.
- (c) Interpret the *y*-intercept of a least squares regression line.
- Organize and describe data graphically. Core Criteria:
 - (a) Create and interpret a box-plot.
 - (b) Create and interpret a histogram.
 - (c) Create and interpret a scatter-plot.
 - (d) Compare multiple graphs for di erent data sets.
 - (e) Determine if data is skewed or symmetric.
 - (f) Create and interpret a bar-plot and stacked or side-by-side bar-plot.

Additional Criteria:

- (a) Create and interpret a dot-plot.
- (b) Create and interpret a steam and leaf diagram.
- (c) Create and interpret a pie chart.
- (d) Create and interpret a cumulative frequency plot.
- (e) Create and interpret side-by-side box plots.
- 4. Calculate and interpret probabilities with discrete distributions using one or more of the following:

Core Criteria:

- (a) Addition rule.
- (b) Multiplication rule.
- (c) Conditional probability.
- (d) Marginal probability.
- (e) Independent events.
- (f) Dependent events
- (g) Compliment.
- (h) Combination.
- (i) Permutation.
- (j) Multiplication law.
- (k) Binomial distribution.
- (I) Mean and standard deviation of the binomial distribution.
- (m) Tree diagram.
- (n) Expected Value

Additional Criteria:

- (a) Probability distribution.
- (b) Law of large numbers.
- (c) Standard deviation of a probability distribution.
- 5. Calculate and interpret probabilities with continuous distributions using one or more of the following distributions or concepts:

Core Criteria:

- (a) Normal Distribution.
- (b) Sampling Distribution of the mean.
- (c) Central limit theorem.
- (d) T-Distribution.

Additional Criteria:

- (a) Proportions.
- 6. Make inferences about population mean(s) using a con dence interval: Core Criteria:
 - (a) Compute con dence intervals for the mean of a large sample (z-value).
 - (b) Compute con dence intervals for the mean of a small sample (t-value).
 - (c) Compute con dence intervals for the di erence of two means. (dependant and independent)
 - (d) Interpret a con dence interval.

Additional Criteria:

- (a) Compute con dence intervals for the mean for a proportion.
- (b) Test hypothesis for one or two proportion(s).
- 7. Make inferences about population mean(s) by hypothesis testing: Core Criteria:
 - (a) Test hypothesis for one or two mean(s).
 - (b) Conduct a one-sample, two-sample or paired *t*-test:

Write the null and alternative hypotheses.

Determine the test statistic t and the degrees of freedom df.

Determine the *P*-value using technology or give an appropriate interval that includes the *P*-value.

Decide whether or not to reject the null hypothesis and write a conclusion.

- (c) Determine whether a *t*-test is one or two-tailed.
- (d) Determine when a paired *t*-test should be used.
- (e) Quantitative evidence from a hypothesis test is conveyed, and explained in such a way that a competent non-expert reader can follow along.